

Tutorial Series 1  
MACHINE STRUCTURE

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Exercise 1:

Use truth tables to prove the following equalities:

1- De Morgan's Theorem:

a-  $\overline{A \cdot B} = \overline{A} + \overline{B}$

b-  $\overline{A+B} = \overline{A} \cdot \overline{B}$

2- The laws of Boolean Algebra: Distributivity:

a-  $A + B \cdot C = (A+B) \cdot (A+C)$

b-  $A \cdot (B+C) = A \cdot B + A \cdot C$

c-  $(A+B) \cdot (\overline{A} \cdot \overline{B}) = 0$

Exercise 2:

Simplify the following functions using boolean algebra laws:

$$F_1 = (a \cdot b + \overline{c}) + c \cdot (\overline{a} + \overline{b})$$

$$F_2 = (a \cdot \overline{b} + c) + (a + \overline{b}) \cdot c$$

$$F_3 = (x+y) \cdot z + \overline{x} \cdot (\overline{y} + z) + \overline{y}$$

$$F_4 = (x + y + z) \cdot (\overline{x} + y + z) + x \cdot y + y \cdot z$$

Exercise 3:

The function F(A,B,C) with three variables is defined by the following truth table:

A	B	C	F
0	0	0	1
0	0	1	1
0	1	0	0
0	1	1	1
1	0	0	1
1	0	1	0
1	1	0	0
1	1	1	1

1- Write the function F in the disjunctive form (first canonical form).

2- Write the function f in the conjunctive form (second canonical form).

3- Write these equations in decimal notation.

Exercise 4:

Convert the following functions to their corresponding canonical form:

$$F_1(A,B) = \sum(0,1)$$

$$F_2(A,B,C) = \prod(0,1,2)$$

$$F_3(A,B,C) = \sum(0,1,3,4,5)$$

**Exercise 5:**

- 1) Give the first canonical form of the Boolean functions defined by the following proposals:
  - a)  $F(A,B,C) = 1$  if and only if one of the variables A, B and C takes the value 0.
  - b)  $F(A,B,C) = 0$  if and only if at least two of the variables A, B and C take the value 1.
  - c)  $F(A,B,C) = B.C + C + A.\bar{B}$
  
- 2) Give the second canonical form of the boolean functions defined by the following proposals:
  - a)  $F(A,B,C) = 0$  if and only if the variables A, B, and C take the value 1 or 0.
  - b)  $F(A,B,C) = 1$  if and only if at most one of the variables A, B and C takes the value 0.
  - c)  $F(A,B,C) = (A+B).(B+\bar{C})$

**Exercise 6:**

Find the complement of the following boolean functions and provide their final simplified functions if possible:

$$F_1 = \bar{A}.\bar{B} + A.(\bar{B} + C) \qquad F_2 = A.\bar{B}.(A+C) + \bar{A}.B. \overline{(A+\bar{B}+\bar{C})}$$

$$F_3 = (A+B.C).(\bar{A}.B+C) \qquad F_4 = (C+D). \overline{A.\bar{C}.D} . (\bar{A}.C+\bar{D})$$