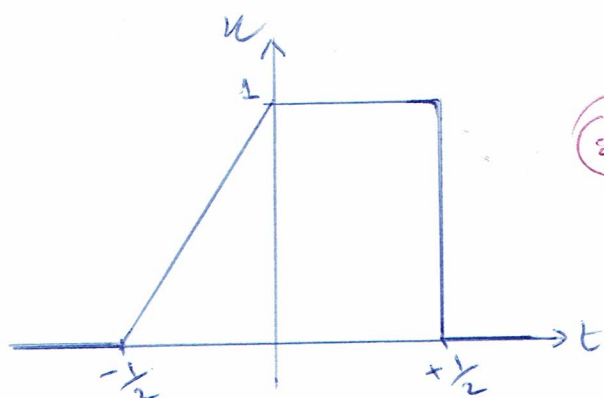


Corrigé type
Interpolation TS

1^o/



2^o/ Densité spectrale pour f=0:

$$X(0) = \int_{-\frac{1}{2}}^0 (2t+1) dt + \int_0^{\frac{1}{2}} 1 dt = \left[\frac{2}{2} \frac{t^2}{2} + t \right]_{-\frac{1}{2}}^0 + [t]_0^{\frac{1}{2}} = 0 - \frac{1}{4} + \frac{1}{2} + \frac{1}{2} = \frac{3}{4}$$

3^o/ Transformée de Fourier:

$$X(f) = \int_{-\infty}^{+\infty} x(t) \cdot e^{-j2\pi f t} dt$$

$$= \underbrace{\int_{-\frac{1}{2}}^0 (2t+1) e^{-j2\pi f t} dt}_A + \underbrace{\int_0^{\frac{1}{2}} e^{-j2\pi f t} dt}_B$$

$$A = (2t+1) \frac{e^{-j2\pi f t}}{-j2\pi f} \Big|_{-\frac{1}{2}}^0 - 2 \frac{e^{-j2\pi f t}}{(-j2\pi f)^2} \Big|_{-\frac{1}{2}}^0$$

$$= -\frac{1}{j2\pi f} - 2 \frac{(1 - e^{j\pi f})}{(j2\pi f)^2}$$

$$B = \frac{1 - e^{-j\pi f}}{j2\pi f}$$

$$\Rightarrow X(f) = -\frac{1}{j2\pi f} + \frac{2e^{j\pi f} - 2}{(j2\pi f)^2} + \frac{1 - e^{-j\pi f}}{j2\pi f} = 2 \frac{e^{j\pi f} - 1}{(j2\pi f)^2} - \frac{e^{-j\pi f}}{j2\pi f}$$