

$$2) \text{ r } > R$$

$$V_2 = -\int E_2 dr = -\int \frac{q}{4\pi\epsilon_0 r^2} dr - \int \frac{R^2 \sigma}{r^2} dr$$

$$V_2 = \frac{q}{4\pi\epsilon_0 r} + \frac{R^2 \sigma}{\epsilon_0 r} + C_2$$

Calcul de C_1, C_2 ?

$$1) V_2(r \rightarrow +\infty) = 0$$

$$2) V_2(r=R) = V_1(r=R)$$

$$V_2(r \rightarrow +\infty) = 0 \Rightarrow C_2 = 0$$

$$V_2(r=R) = V_1(r=R)$$

$$\frac{q}{4\pi\epsilon_0 R} + \frac{R^2 \sigma}{\epsilon_0 R} = \frac{q}{4\pi\epsilon_0 R} + C_1$$

$$C_1 = \frac{R\sigma}{\epsilon_0}$$

$$\text{Donc : } \begin{cases} V_1 = \frac{q}{4\pi\epsilon_0 r} + \frac{R\sigma}{\epsilon_0} \\ V_2 = \frac{q}{4\pi\epsilon_0 r} + \frac{\sigma R^2}{\epsilon_0 r} \end{cases}$$