

## Condition Limite gauche de Neumann discrétisée par un schéma centré

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> restart : with(LinearAlgebra) :
> L := 20; H := 20; ndx := 3; ndy := 3;
          L:=20
          H:=20
          ndx:=3
          ndy:=3
(1.1)

> Td := 10; Tb := 10; Th := 30; alpha := 0
          Td:=10
          Tb:=10
          Th:=30
          alpha:=0
(1.2)

> Delta_x := L / ndx; Delta_y := H / ndy; beta := Delta_x / Delta_y
          Delta_x:=20/3
          Delta_y:=20/3
          beta:=1
(1.3)

> i_max := ndx + 1; j_max := ndy + 1;
          i_max:=4
          j_max:=4
(1.4)

> N := (i_max - 2) * (j_max - 2) + j_max - 2;
          N:=6
(1.5)

> for j from 2 to j_max - 1 do T[i_max, j] := Td end do;
          T[4, 2]:=10
          T[4, 3]:=10
(1.6)

> for i from 1 to i_max - 1 do T[i, 1] := Tb end do;
          T[1, 1]:=10
          T[2, 1]:=10
          T[3, 1]:=10
(1.7)

> for i from 1 to i_max - 1 do T[i, j_max] := Th end do;
          T[1, 4]:=30
          T[2, 4]:=30
          T[3, 4]:=30
(1.8)

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k := 1 :
  for j from 2 to  $j_{\max} - 1$  do
     $T[0, j] := T[2, j] - 2 \cdot \alpha \cdot \Delta x :$ 
     $Eq[k] := -2 \cdot (1 + \beta^2) \cdot T[1, j] + T[2, j] + T[0, j] + \beta^2 \cdot (T[1, j+1] + T[1, j-1]) = 0 :$ 
     $TempS[k] := T[1, j] :$ 
    k := k + 1 :
    for i from 2 to  $i_{\max} - 1$  do
       $Eq[k] := -2 \cdot (1 + \beta^2) \cdot T[i, j] + T[i+1, j] + T[i-1, j] + \beta^2 \cdot (T[i, j+1] + T[i, j-1]) = 0 :$ 
       $TempS[k] := T[i, j] :$ 
      k := k + 1 :
    end do
end do:

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$$\begin{aligned}
&> \text{for } k \text{ from } 1 \text{ to } N \text{ do } Eq[k] \text{ end do;} \\
&\quad -4 T_{1,2} + 2 T_{2,2} + T_{1,3} + 10 = 0 \\
&\quad -4 T_{2,2} + T_{3,2} + T_{1,2} + T_{2,3} + 10 = 0 \\
&\quad -4 T_{3,2} + 20 + T_{2,2} + T_{3,3} = 0 \\
&\quad -4 T_{1,3} + 2 T_{2,3} + 30 + T_{1,2} = 0 \\
&\quad -4 T_{2,3} + T_{3,3} + T_{1,3} + 30 + T_{2,2} = 0 \\
&\quad -4 T_{3,3} + 40 + T_{2,3} + T_{3,2} = 0 \tag{1.9}
\end{aligned}$$

$$\begin{aligned}
&> N := k - 1; \\
&\quad N := 6 \tag{1.10}
\end{aligned}$$

$$\begin{aligned}
&> Eqs := \{ seq(Eq[k], k = 1 .. N) \}; \\
Eqs := & \{ -4 T_{1,2} + 2 T_{2,2} + T_{1,3} + 10 = 0, -4 T_{1,3} + 2 T_{2,3} + 30 + T_{1,2} = 0, -4 T_{3,2} + 20 \\
& + T_{2,2} + T_{3,3} = 0, -4 T_{3,3} + 40 + T_{2,3} + T_{3,2} = 0, -4 T_{2,2} + T_{3,2} + T_{1,2} + T_{2,3} + 10 \\
& = 0, -4 T_{2,3} + T_{3,3} + T_{1,3} + 30 + T_{2,2} = 0 \} \tag{1.11}
\end{aligned}$$

$$\begin{aligned}
&> Tmps := [ seq(TempS[k], k = 1 .. N) ]; \\
&\quad Tmps := [ T_{1,2}, T_{2,2}, T_{3,2}, T_{1,3}, T_{2,3}, T_{3,3} ] \tag{1.12}
\end{aligned}$$

$$\begin{aligned}
&> SolT := solve(Eqs, Tmps); \\
SolT := & \left[ \left[ T_{1,2} = \frac{1546}{99}, T_{2,2} = \frac{500}{33}, T_{3,2} = \frac{1334}{99}, T_{1,3} = \frac{2194}{99}, T_{2,3} = \frac{710}{33}, T_{3,3} \right. \right. \\
& \left. \left. = \frac{1856}{99} \right] \right] \tag{1.13}
\end{aligned}$$

$$\begin{aligned}
&> Eqs := [ seq(Eq[k], k = 1 .. N) ]; \\
Eqs := & [ -4 T_{1,2} + 2 T_{2,2} + T_{1,3} + 10 = 0, -4 T_{2,2} + T_{3,2} + T_{1,2} + T_{2,3} + 10 = 0, -4 T_{3,2} \\
& + 20 + T_{2,2} + T_{3,3} = 0, -4 T_{1,3} + 2 T_{2,3} + 30 + T_{1,2} = 0, -4 T_{2,3} + T_{3,3} + T_{1,3} \\
& + 30 + T_{2,2} = 0, -4 T_{3,3} + 40 + T_{2,3} + T_{3,2} = 0 ] \tag{1.14}
\end{aligned}$$

> M, R := GenerateMatrix(Eqs, Tmps)

$$M, R := \left[ \begin{array}{cccccc} -4 & 2 & 0 & 1 & 0 & 0 \\ 1 & -4 & 1 & 0 & 1 & 0 \\ 0 & 1 & -4 & 0 & 0 & 1 \\ 1 & 0 & 0 & -4 & 2 & 0 \\ 0 & 1 & 0 & 1 & -4 & 1 \\ 0 & 0 & 1 & 0 & 1 & -4 \end{array} \right], \left[ \begin{array}{c} -10 \\ -10 \\ -20 \\ -30 \\ -30 \\ -40 \end{array} \right] \quad (1.15)$$