

Conditions Limites gauche et droite de Neumann discrétisée par un schéma centré

```

> restart : with(LinearAlgebra) :
> L := 6; H := 6; ndx := 3; ndy := 3;
      L:=6
      H:=6
      ndx:=3
      ndy:=3
                                         (1.1)

> Tb := 100; Th := 40; α[g] := 10; α[d] := 20
      Tb := 100
      Th := 40
      αg := 10
      αd := 20
                                         (1.2)

> Δx :=  $\frac{L}{ndx}$ ; Δy :=  $\frac{H}{ndy}$ ; β :=  $\frac{\Delta x}{\Delta y}$ 
      Δx := 2
      Δy := 2
      β := 1
                                         (1.3)

> imax := ndx + 1; jmax := ndy + 1;
      imax := 4
      jmax := 4
                                         (1.4)

> N := (imax - 2) · (jmax - 2) + 2 · (jmax - 2);
      N := 8
                                         (1.5)

>
                                         (1.6)

> for i from 1 to imax do T[i, 1] := Tb end do;
      T1, 1 := 100
      T2, 1 := 100
      T3, 1 := 100
      T4, 1 := 100
                                         (1.7)

> for i from 1 to imax do T[i, jmax] := Th end do;
      T1, 4 := 40
      T2, 4 := 40
      T3, 4 := 40
      T4, 4 := 40
                                         (1.8)

```

```

k := 1 :
for j from 2 to  $j_{\max} - 1$  do
     $T[0, j] := T[2, j] - 2 \cdot \alpha[g] \cdot \Delta x :$ 
     $Eq[k] := -2 \cdot (1 + \beta^2) \cdot T[1, j] + T[2, j] + T[0, j] + \beta^2 \cdot (T[1, j+1] + T[1, j-1]) = 0 :$ 
     $TempS[k] := T[1, j] :$ 
    k := k + 1 :
    for i from 2 to  $i_{\max} - 1$  do
         $Eq[k] := -2 \cdot (1 + \beta^2) \cdot T[i, j] + T[i+1, j] + T[i-1, j] + \beta^2 \cdot (T[i, j+1] + T[i, j-1]) = 0 :$ 
         $TempS[k] := T[i, j] :$ 
        k := k + 1 :
    end do:
     $T[i_{\max} + 1, j] := T[i_{\max} - 1, j] + 2 \cdot \alpha[d] \cdot \Delta x :$ 
     $Eq[k] := -2 \cdot (1 + \beta^2) \cdot T[i_{\max}, j] + T[i_{\max} - 1, j] + T[i_{\max} + 1, j] + \beta^2 \cdot (T[i_{\max}, j+1] + T[i_{\max}, j-1]) = 0 :$ 
     $TempS[k] := T[i_{\max}, j] :$ 
    k := k + 1 :
end do: =

```

$$\begin{aligned}
& > \text{for } k \text{ from } 1 \text{ to } N \text{ do } Eq[k] \text{ end do;} \\
& \quad -4 T_{1,2} + 2 T_{2,2} + 60 + T_{1,3} = 0 \\
& \quad -4 T_{2,2} + T_{3,2} + T_{1,2} + T_{2,3} + 100 = 0 \\
& \quad -4 T_{3,2} + T_{4,2} + T_{2,2} + T_{3,3} + 100 = 0 \\
& \quad -4 T_{4,2} + 2 T_{3,2} + 180 + T_{4,3} = 0 \\
& \quad -4 T_{1,3} + 2 T_{2,3} + T_{1,2} = 0 \\
& \quad -4 T_{2,3} + T_{3,3} + T_{1,3} + 40 + T_{2,2} = 0 \\
& \quad -4 T_{3,3} + T_{4,3} + T_{2,3} + 40 + T_{3,2} = 0 \\
& \quad -4 T_{4,3} + 2 T_{3,3} + 120 + T_{4,2} = 0 \tag{1.9}
\end{aligned}$$

$$> N := k - 1; \quad N := 8 \tag{1.10}$$

$$\begin{aligned}
& > Eqs := \{ seq(Eq[k], k = 1 .. N) \}; \\
& Eqs := \{ -4 T_{1,3} + 2 T_{2,3} + T_{1,2} = 0, -4 T_{1,2} + 2 T_{2,2} + 60 + T_{1,3} = 0, -4 T_{4,2} + 2 T_{3,2} \\
& \quad + 180 + T_{4,3} = 0, -4 T_{4,3} + 2 T_{3,3} + 120 + T_{4,2} = 0, -4 T_{2,2} + T_{3,2} + T_{1,2} + T_{2,3} \\
& \quad + 100 = 0, -4 T_{2,3} + T_{3,3} + T_{1,3} + 40 + T_{2,2} = 0, -4 T_{3,2} + T_{4,2} + T_{2,2} + T_{3,3} \\
& \quad + 100 = 0, -4 T_{3,3} + T_{4,3} + T_{2,3} + 40 + T_{3,2} = 0 \} \tag{1.11}
\end{aligned}$$

$$> Tmps := [seq(TempS[k], k = 1 .. N)];
\quad Tmps := [T_{1,2}, T_{2,2}, T_{3,2}, T_{4,2}, T_{1,3}, T_{2,3}, T_{3,3}, T_{4,3}] \tag{1.12}$$

$$\begin{aligned}
& > SolT := solve(Eqs, Tmps);
& SolT := [[T_{1,2} = 66, T_{2,2} = 79, T_{3,2} = 91, T_{4,2} = 114, T_{1,3} = 46, T_{2,3} = 59, T_{3,3} = 71, T_{4,3} \\
& \quad = 94]] \tag{1.13}
\end{aligned}$$

```

> Eqs := [seq(Eq[k], k = 1 .. N)];
Eqs := [ -4 T1,2 + 2 T2,2 + 60 + T1,3 = 0, -4 T2,2 + T3,2 + T1,2 + T2,3 + 100 = 0,
          -4 T3,2 + T4,2 + T2,2 + T3,3 + 100 = 0, -4 T4,2 + 2 T3,2 + 180 + T4,3 = 0, -4 T1,3
          + 2 T2,3 + T1,2 = 0, -4 T2,3 + T3,3 + T1,3 + 40 + T2,2 = 0, -4 T3,3 + T4,3 + T2,3
          + 40 + T3,2 = 0, -4 T4,3 + 2 T3,3 + 120 + T4,2 = 0 ]

```

```
> M, R := GenerateMatrix(Eqs, Tmps)
```

$$M, R := \left[\begin{array}{ccccccccc} -4 & 2 & 0 & 0 & 1 & 0 & 0 & 0 & -60 \\ 1 & -4 & 1 & 0 & 0 & 1 & 0 & 0 & -100 \\ 0 & 1 & -4 & 1 & 0 & 0 & 1 & 0 & -100 \\ 0 & 0 & 2 & -4 & 0 & 0 & 0 & 1 & -180 \\ 1 & 0 & 0 & 0 & -4 & 2 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 1 & -4 & 1 & 0 & -40 \\ 0 & 0 & 1 & 0 & 0 & 1 & -4 & 1 & -40 \\ 0 & 0 & 0 & 1 & 0 & 0 & 2 & -4 & -120 \end{array} \right], \quad (1.15)$$