

2^{ème} Année Licence ELM

CORRIGE TYPE
RESISTANCE DES MATERIAUX (RDM)

Semestre : 04 (2021-2022)

Exercice N01 (6pts)

Données :

- $d = 24 \text{ mm}$ $F = 8.10^4 \text{ N}$

Contrainte de cisaillement du boulon

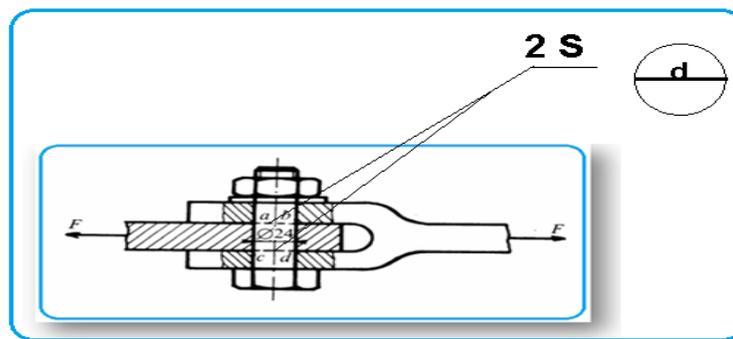


Figure 1

On a :

$$\tau = T/S_t \dots (A) \quad (1)$$

Avec :

$$T = F \dots (a)$$

$$S_t = 2S = 2 \left(\Pi \frac{d^2}{4} \right) = \left(\Pi \frac{d^2}{2} \right) \dots (b) \quad (2)$$

(a) et (b) dans (A) donne :

$$\tau = F / \left(\Pi \frac{d^2}{2} \right) \quad (1)$$

$$\text{AN/} \quad \tau = 8.10^4 / \left(\Pi \frac{24^2}{2} \right)$$

$$\tau = 88.41 \text{ MPa} \quad (2)$$

Exercice N 02 (14pts)

Données :

$F_1 = 45 \text{ KN}$ et $F_3 = 450 \text{ KN}$

$S_1 = 625 \text{ mm}^2$, $S_2 = 2500 \text{ mm}^2$ et $S_3 = 1250 \text{ mm}^2$

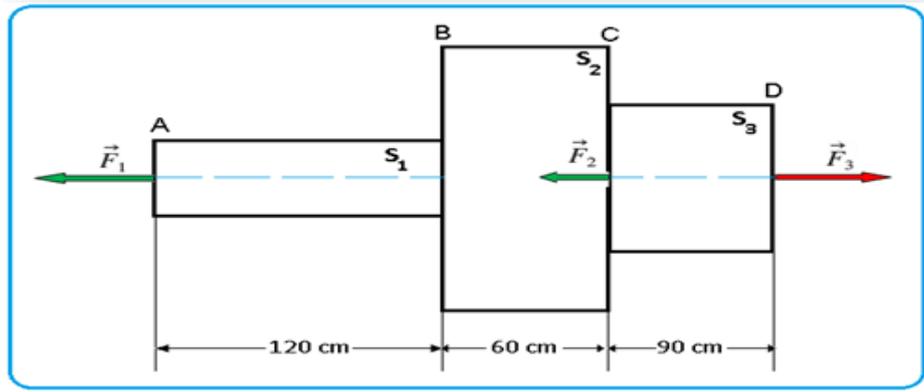


Figure 2

1- Valeur de l'effort F_2

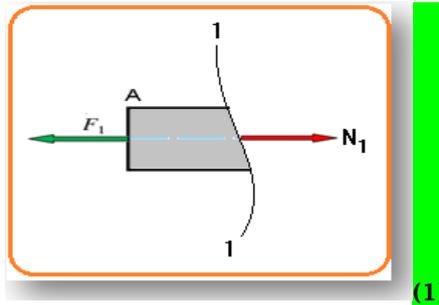
Equilibre de l'arbre : $\vec{F}_1 + \vec{F}_2 + \vec{F}_3 = \vec{0}$

Ox : $-F_1 - F_2 + F_3 = 0 \Rightarrow F_2 = 450 - 45$ (0.5)

$\Rightarrow F_2 = 405 \text{ KN}$ (1)

2/- Contrainte normale maximale σ dans l'arbre

- Coupure 1-1 : $0 < x < 120 \text{ cm}$ (0.5)



(1)

$\sum F = 0 \Rightarrow N_1 - 45 = 0$

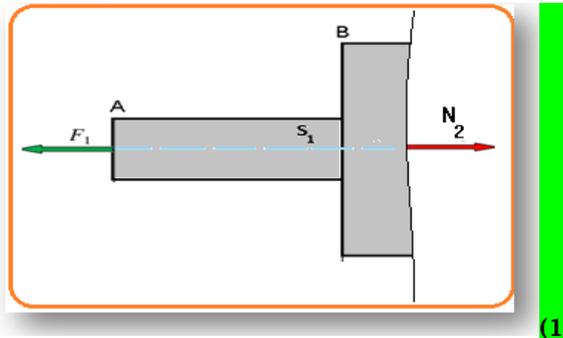
$\Rightarrow N_1 = 45 \text{ KN}$ (0.5)

$N_1 > 0$ traction (0.5)

$\sigma_1 = \frac{N_1}{S_1} = \frac{45 \times 10^3}{625} \Rightarrow \sigma_1 = 72 \text{ N/mm}^2$ (0.5)

$\sigma_1 = 72 \text{ MPa}$ (0.5)

Coupure 2-2 : $120 \text{ cm} < x < 180 \text{ cm}$ (0.5)



(1)

$\sum F = 0 \Rightarrow N_2 - 45 = 0$

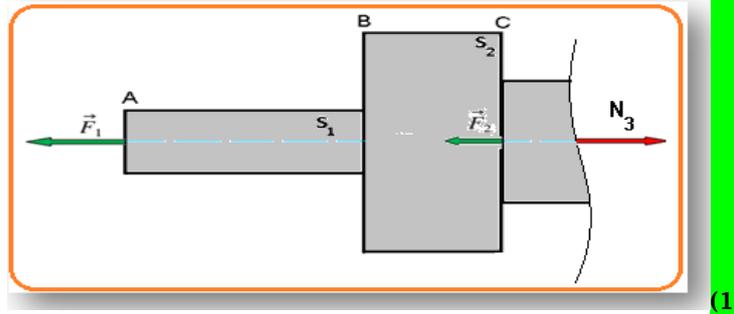
$$\Rightarrow N_2 = 45 \text{ KN (0.5)}$$

$$N_2 > 0 \text{ traction (0.5)}$$

$$\nabla_2 = \frac{N_2}{S} \Rightarrow \nabla_2 = \frac{45 \times 10^3}{2500} = 18 \text{ N/mm}^2 \text{ (0.5)}$$

$$\Rightarrow \nabla_2 = 18 \text{ MPa (0.5)}$$

Coupure 3-3 : $180 \text{ cm} < x < 270 \text{ cm}$ (0.5)



$$\sum F = 0 \Rightarrow -F_1 - F_2 + N_3 = 0 \Rightarrow N_3 = F_1 + F_2$$

$$\Rightarrow N_3 = 45 + 405$$

$$\Rightarrow N_3 = 450 \text{ KN (0.5)}$$

$$N_3 > 0 \text{ traction (0.5)}$$

$$\nabla_3 = \frac{N_3}{S_3} \Rightarrow \nabla_3 = \frac{450 \times 10^3}{1250}$$

$$\Rightarrow \nabla_3 = 360 \text{ N/mm}^2 \text{ (0.5)}$$

On a : $\nabla_1 = 72 \text{ N/mm}^2$ $\nabla_2 = 180 \text{ N/mm}^2$

$$\nabla_3 = 360 \text{ MPa (0.5)}$$

La valeur de la contrainte maximale est :

$$\nabla_{max} = \nabla_3 = 360 \text{ N/mm}^2 \text{ (1)}$$

$$\nabla_{max} = \nabla_3 = 360 \text{ MPa (1)}$$